## Linear Algebra II - Worksheet 6

In  $\mathbb{R}^3$ , we consider the plane V of equation  $x_1 + x_2 - x_3 = 0$ .

- 1. Compute  $V^{\perp}$ .
- 2. Find an orthonormal basis  $\mathcal{B}_V$  of V.
- 3. Complete  $\mathscr{B}_V$  into an orthonormal basis  $\mathscr{B}$  of  $\mathbb{R}^3$ .
- 4. Prove that there is a rotation T around the axis  $V^{\perp}$  and angle  $\pi/3$  such that

$$T \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}.$$

Compute  $[T]_{\mathscr{B}}^{\mathscr{B}}$ .

5. Compute [T].