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**Membership of academic societies:**

Mathematical Society of Japan

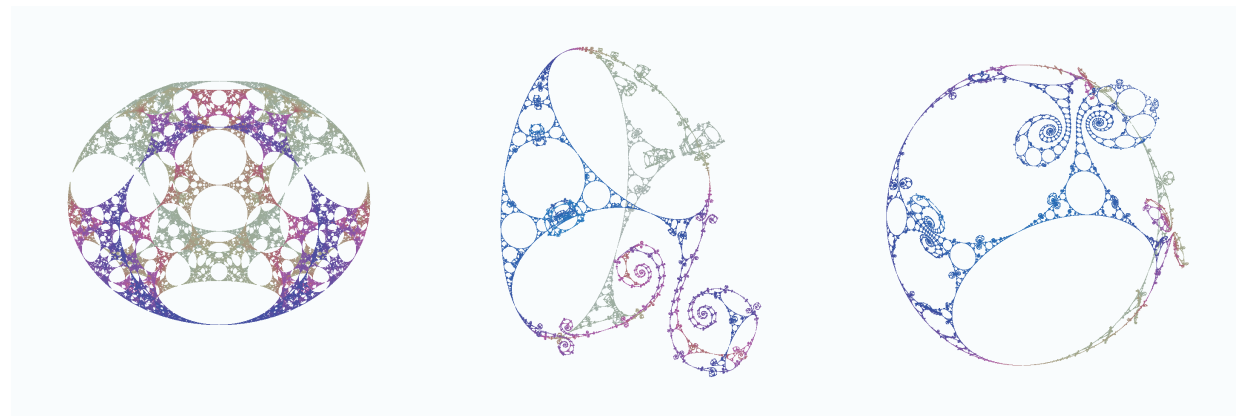
**Research Interest:**

- Hyperbolic geometry, conformal Geometry
- Kleinian groups, Riemann surfaces, Teichmüller theory
- Low-dimensional topology

**Research Summary:**

My major research interest is hyperbolic geometry. Especially I am interested in hyperbolic 3-manifolds and their deformation spaces. A hyperbolic 3-manifold is obtained as the quotient manifold of the hyperbolic 3-space by the action of a Kleinian group, a discrete subgroup of  $\mathrm{PSL}(2, \mathbb{C})$ . The boundary of the deformation space of a Kleinian group has fractal structure, and is very complicated. I am eager to understand the ‘complexity’ of the boundaries of these spaces.

I also interested in higher dimensional Kleinian groups, especially 4-dimensional Kleinian groups acting on the hyperbolic 4-space. In this case, limit sets of Kleinian groups are fractal objects in 3-sphere. Figures below are computer-generated limit sets of 4-dimensional Kleinian groups with two generators.



**Major Publications:**

- [1] K. Ito, *Convergence and divergence of Kleinian punctured torus groups*, Amer. J. Math. 134 (2012), 861–889.
- [2] Y. Araki and K. Ito, *An extension of the Maskit slice for 4-dimensional Kleinian groups*, Conform. Geom. Dyn. 12 (2008), 199–226.
- [3] K. Ito, *On continuous extensions of grafting maps*, Trans. Amer. Math. Soc. 360 (2008), 3731–3749.

- [4] K. Ito, *Exotic projective structures and quasi-Fuchsian space, II*, Duke Math. J. 140 (2007), 85–109.
- [5] K. Ito, *Schottky groups and Bers boundary of Teichmüller space*, Osaka J. Math. 40 (2003), 639–657.
- [6] K. Ito, *Exotic projective structures and quasi-Fuchsian space*, Duke Math. J. 105 (2000), 185–209.

### Education and Appointments:

- 2000 Ph.D. at Tokyo Institute of Technology
- 2000 Assistant Professor, Nagoya University
- 2007 Associate Professor, Nagoya University

### Message to Prospective Students:

Some basic references of this area are [1], [2] and [3]. More advanced topics can be found in [4], [5], [6] and [7]. Especially [5] is the best reference to get an impression of this area. Some master course students used [3], [8], [9] and [10] as textbooks of seminar. [11] will be used in the forthcoming master course seminar. [12] is a good guidebook for drawing computer graphics as in the previous page. Students who are interested in such computer graphics are also welcome.

- [1] S. Katok, *Fuchsian Groups*, The University of Chicago Press, 1992.
- [2] F. Bonahon, *Low-dimensional geometry: from euclidean surfaces to hyperbolic knots*, AMS, 2009.
- [3] A. F. Beardon, *The geometry of Discrete Groups*, Springer GTM 91, 1983.
- [4] A. Marden, *Outer Circles*, Cambridge University Press, 2007.
- [5] K. Matsuzaki and M. Taniguchi, *Hyperbolic Manifolds and Kleinian Groups*, Oxford Science Publications, 1998.
- [6] Y. Imayoshi and M. Taniguchi, *An Introduction to Teichmüller Spaces*, Springer, 1992.
- [7] A. Fathi, F. Laudenbach and V. Poenaru, (translated by D. M. Kim and D. Margalit) *Thurston’s work on surfaces*, Princeton University Press 2012.
- [8] K. Stephenson, *Introduction to Circle Packing*, Cambridge University Press, 2005.
- [9] P. J. Notholls, *The Ergodic Theory of Discrete Groups*, Cambridge University Press, 1989.
- [10] F. Dal’Bo, *Geodesic and Horocyclic Trajectories*, Springer, 2011.
- [11] B. Farb and D. Margalit, *A Primer on Mapping Class Groups*, Princeton University Press, 2012.
- [12] D. Mumford, C. Series, D. Wright, *Indra’s Pearls*, Cambridge University Press, 2002.